## Present Value

Mariah Carey deal. what were they thinking?

## Calculate that deal

backwards loan calc usage read mixerman diaries

The agent escrow account. book keeping

## Homework

Future value calculation.....

FV of $\$ 25,000$ loan. 2 years. 8 percent annual interest. calculated monthly.
FV of $\$ 25,000$ loan. 2 years 8 percent interest calculated quarterly.
FV of \$1000 loan. 6 months. $25 \%$ annual interest calculated daily.

Generate a loan amortization table for a $\$ 5000$ loan. Annual interest II\%, Length of loan is 18 months and payments are monthly. make a pdf, screen shot or other digital file. print it out or if you must email it to me.
due tuesday at 5:00 pm

8 percent annual interest monthly calculation 8/I2\%= . 00666666667

## 2 years in months $=24$ months

$$
F V=25000(1+.0067)^{24}=29322.20
$$

8 percent interest calculated quartely

$$
8 \% / 4=.02
$$

2 years of quarters $=8$ time periods

$$
F V=25000(1+.02)^{8}=29291.48
$$

FV calculated more often is more! FV calculated less often is less!

FV of $\$ 1000$ loan. 6 months. $25 \%$ annual interest calculated daily.
$25 \%$ annual interest $=0.0006849$ daily interest
6 months has 182.5 days

$$
F V=1000(1+0.0006849)^{182.5}=1133.09
$$

Assuming 365 days a year.
this is what your credit card is probably charging you

## Amortization Calculator

Almost any data field on this form may be calculated. Enter the appropriate numbers in each slot, leaving blank (or zero) the value that you wish to determine, and then click "Calculate" to update the page.


This loan calculator is written and maintained by Bret Whissel.
See Bret's Blog for help, a spreadsheet, derivations, calculator news, and more information.

## Summary

Principal borrowed: $\$ 5,000.00$
Regular Payment amount: \$302.59 Final Balloon Payment: \$0.05
Interest-only payment: \$45.83

Annual Payments: 12
Total Payments: 19 (1.58 years)
Annual interest rate: $11.00 \%$
Periodic interest rate: $0.9167 \%$

| Pmt | Principal | Interest | Cum Prin | Cum Int | Prin Bal |
| :---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 256.76 | 45.83 | 256.76 | 45.83 | $4,743.24$ |
| 2 | 259.11 | 43.48 | 515.87 | 89.31 | $4,484.13$ |
| 3 | 261.49 | 41.10 | 777.36 | 130.41 | $4,222.64$ |
| 4 | 263.88 | 38.71 | $1,041.24$ | 169.12 | $3,958.76$ |
| 5 | 266.30 | 36.29 | $1,307.54$ | 205.41 | $3,692.46$ |
| 6 | 268.74 | 33.85 | $1,576.28$ | 239.26 | $3,423.72$ |
| 7 | 271.21 | 31.38 | $1,847.49$ | 270.64 | $3,152.51$ |
| 8 | 273.69 | 28.90 | $2,121.18$ | 299.54 | $2,878.82$ |
| 9 | 276.20 | 26.39 | $2,397.38$ | 325.93 | $2,602.62$ |
| 10 | 278.73 | 23.86 | $2,676.11$ | 349.79 | $2,323.89$ |
| 11 | 281.29 | 21.30 | $2,957.40$ | 371.09 | $2,042.60$ |
| 12 | 283.87 | 18.72 | $3,241.27$ | 389.81 | $1,758.73$ |
| 13 | 286.47 | 16.12 | $3,527.74$ | 405.93 | $1,472.26$ |
| 14 | 289.09 | 13.50 | $3,816.83$ | 419.43 | $1,183.17$ |
| 15 | 291.74 | 10.85 | $4,108.57$ | 430.28 | 891.43 |
| 16 | 294.42 | 8.17 | $4,402.99$ | 438.45 | 597.01 |
| 17 | 297.12 | 5.47 | $4,700.11$ | 443.92 | 299.89 |
| 18 | 299.84 | 2.75 | $4,999.95$ | 446.67 | 0.05 |
| 19 | $* 0.05$ | 0.00 | $5,000.00$ | 446.67 | 0.00 |

What is the present value of a lump sum of money in the future?

What is the present value of a stream of monthly payments (example pension, royalties etc) in the future?

Why would you need to know this?
Divorce! Any of you going in to family law or accounting will eventually encounter this problem.

Buying out a partner in a business.
Buying out a member of the band.
Value of a life insurance policy.
Getting an advance against royalties owed in the future?

## Remember this equation

$\mathrm{FV}=\mathrm{PV} *(1+\mathrm{i})^{n}$
This implies
$\mathrm{PV}=\mathrm{FV} /(1+\mathrm{i})^{n}$
As usual
PV is present value
FV is Future value
i is the interest rate per period
and n is the number of periods.

What interest rate do we use?
Interest rate represents the market expectation of inflation + risk.
If we assume this amount is risk free the only thing the interest rate represents is expectations of inflation.
in this case use the interest rate for US treasuries for that period of time.
www.treasury.gov/resource-center/data-chart-center/interest-rates/Pages/TextView.aspx?data=yield

| To access interest rate data in the legacy XML format, click here. |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Select type of Interest Rate Data |  |  |  |  |  |  |  |  |  |  |  |
| Daily Treasury Yield Curve Rates $\quad$ Go |  |  |  |  |  |  |  |  |  |  |  |
| Select Time Period |  |  |  |  |  |  |  |  |  |  |  |
| Current Month Go |  |  |  |  |  |  |  |  |  |  |  |
| Date | 1 Mo | 3 Mo | 6 Mo | $\begin{gathered} 1 \mathrm{Yr} \\ \text { auth (2).uad2 } \end{gathered}$ | 2 Yr | 3 Yr | 5 Yr | 7 Yr | 10 Yr | 20 Yr | 30 Yr |
| 10/03/11 | 0.01 | 0.02 | 0.06 | 0.12 | 0.24 | 0.39 | 0.87 | 1.33 | 1.80 | 2.51 | 2.76 |
| 10/04/11 | 0.01 | 0.01 | 0.04 | 0.11 | 0.25 | 0.40 | 0.90 | 1.35 | 1.81 | 2.53 | 2.77 |
| 10/05/11 | 0.00 | 0.00 | 0.03 | 0.10 | 0.25 | 0.43 | 0.96 | 1.45 | 1.92 | 2.62 | 2.87 |
| 10/06/11 | 0.01 | 0.01 | 0.03 | 0.09 | 0.29 | 0.46 | 1.01 | 1.52 | 2.01 | 2.71 | 2.96 |
| 10/07/11 | 0.01 | 0.01 | 0.04 | 0.11 | 0.30 | 0.50 | 1.08 | 1.61 | 2.10 | 2.78 | 3.02 |
| 10/11/11 | 0.01 | 0.02 | 0.05 | 0.12 | 0.32 | 0.54 | 1.14 | 1.68 | 2.18 | 2.87 | 3.11 |
| 10/12/11 | 0.01 | 0.02 | 0.06 | 0.09 | 0.29 | 0.54 | 1.17 | 1.72 | 2.24 | 2.94 | 3.19 |
| 10/13/11 | 0.02 | 0.02 | 0.05 | 0.11 | 0.29 | 0.51 | 1.11 | 1.67 | 2.19 | 2.90 | 3.15 |
| 10/14/11 | 0.02 | 0.02 | 0.06 | 0.11 | 0.28 | 0.50 | 1.12 | 1.71 | 2.26 | 2.97 | 3.22 |

* 30-year Treasury constant maturity series was discontinued on February 18, 2002 and reintroduced on February 9, 2006. From February 18, 2002 to February 8, 2006, Treasury published alternatives to a 30 -year rate. See Long-Term Average Rate for more information.

Treasury discontinued the 20-year constant maturity series at the end of calendar year 1986 and reinstated that series on October 1, 1993. As a result, there are no 20-year rates available for the time period January 1, 1987 through September 30, 1993.

Treasury Yield Curve Rates. These rates are commonly referred to as "Constant Maturity Treasury" rates, or CMTs. Yields are interpolated by

Interest rates are artificially low. so these PV calculations are probably to high. If i were buying a future lumps sum of money I wouldn't value them this way.
absolutely risk free $\$ 100,000$ due 30 years from now. we always calculate interest calculated annually when we are calculating a lump sum.

```
treasury 30 year yield is 3.22% (per year)
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$$
P V=100,000 /(1+.0322)^{30}=38644.20
$$

Calculate PV of 5000 dollars (risk free) payable 10 years from now. 10 year treasury is \%2.26

$$
P V=5000 /(1+.0226)^{10}=3998.64
$$

## France vs Greece

More risk results in those countries paying a lot higher interest rate than the expected rate based on inflation. There is more risk.
$\$ 10,000$ from the government of Greece due 10 years from now. compare that to
$\$ 10,000$ from the government of France due 10 years from now.

# Greece 10 year yield $=26.9 \%$ French 10 year yield =3.017\% 

$$
P V=10,000 /(1+.269)^{10}=923.38
$$

$$
P V=10,000 /(1+.0317)^{10}=7319.23
$$

NOTE! these are not bonds. bonds include quarterly interest.if these were bonds it'd have a different value. For instance a 10,000 euro bond issued by government of greece is currently valued by the markets at about $\$ 2400$. the interest payments make this a much more complicated present value calculatoion

As the interest rate increases PV decreases As the interest rate decreases PV increases
also note
As the interest rate increases FV increases AS the interest rate decreases FV decreases
Q.How do we calculate PV for an individual or entity?

There is no market to "price" their debt to suggest an interest rate.
A. We guess or estimate.

Example l'm gonna give you $\$ 1000$ dollars a year from now. But i'm known to sometimes not pay my debts. You guess there is a I/4 chance of me not paying you. So to value this right now you would calculate PV using a interest rate of $25 \%+$ a little more to take into account inflation.

Or consider that David Barbe is gonna give you $\$ 1000$ a year from now. David is known to almost always pay his debts. you guess there is only a slight chance he will be unable to pay. Say $3 \%$. To value this promise right now you would calculate PV using the interest rate of $3 \%+$ a little more to account for inflation.

## PV of DB \$1000 > PV of DL \$1000

## PV of stream of income

My BMI airplay royalty statements average about $\$ 6000$ a quarter. How do i calculate the PV of the next 3 years of BMI statements?


Note that $\$ 72,000$ is total is paid. to $\$ 65,445$. this stream has been "discounted".
How did i get 6\%? i just guessed. i guessed that it's pretty likely to receive an average of $\$ 6000$ each quarter.

Also since this is music we are talking about, my BMI income is susceptible to positive Black Swans so this is actually likely to be undervalued.
*positive black swan? A song from my catalogue get's covered by some huge star? a song from my catalogue becomes the title song to a huge film.

Well actually that's not quite true. I treated my income as a stock and did a historical volatility analysis of it. But we'll save that for the graduate school version of this course.

This is simple way for someone buying my BMI royalties for 3 years to figure out what to offer me for that stream of income.

What if i you decided that their was a lot more variation or risk in that stream of inome. You would use a higher interst rate.

The first four Camper Van Beethoven Records generate an average of $\$ 12,000$ in royalties a year (to CVB). The licensing deal expires soon. Assume we don't want to release these ourselves. What is the PV of 5 years of $\$ 12000$ a year?

If I use I0\% annual interest rate?
If I use $5 \%$ ?
If I use 20\%

## Mariah Careys \$80,000,000 deal**



## needs to generate 3.52 million a quarter plus cover all manufacture and distribution costs

of course typical record deal is usually not a lump sum. 7 years, 7 albums 7 advances. probably something like 15-20million upfront.
so average sales of abut 350,000 albums a quarter. not impossible but pretty unreasonable.

## Homework

PV of a risk free 2000 dollars paid to you 7 years from now. you'll have to find 7 year us treasury rate or "yield"

PV of a stream of income. The income averages 4675 a quarter. 5 years. use an interest rate of $10 \%$. calculate again with an interest rate of 20\%. use the online mortgage calculator to do this.

